

**A7****A Brief Table of Integrals**

The formulas below are stated in terms of constants  $a$ ,  $b$ ,  $c$ ,  $m$ ,  $n$ , and so on. These constants can usually assume any real value and need not be integers. Occasional limitations on their values are stated with the formulas. Formula 5 requires  $n \neq -1$ , for example, and Formula 11 requires  $n \neq -2$ . The formulas also assume that the constants do not take on values that require dividing by zero or taking even roots of negative numbers. For example, Formula 8 assumes  $a \neq 0$ , and Formula 13(a) cannot be used unless  $b$  is negative.

1.  $\int u \, dv = uv - \int v \, du$

2.  $\int a^u \, du = \frac{a^u}{\ln a} + C, \quad a \neq 1, \quad a > 0$

3.  $\int \cos u \, du = \sin u + C$

4.  $\int \sin u \, du = -\cos u + C$

5.  $\int (ax + b)^n \, dx = \frac{(ax + b)^{n+1}}{a(n+1)} + C, \quad n \neq -1$

6.  $\int (ax + b)^{-1} \, dx = \frac{1}{a} \ln |ax + b| + C$

7.  $\int x(ax + b)^n \, dx = \frac{(ax + b)^{n+1}}{a^2} \left[ \frac{ax + b}{n+2} - \frac{b}{n+1} \right] + C, \quad n \neq -1, -2$

8.  $\int x(ax + b)^{-1} \, dx = \frac{x}{a} - \frac{b}{a^2} \ln |ax + b| + C$

9.  $\int x(ax + b)^{-2} \, dx = \frac{1}{a^2} \left[ \ln |ax + b| + \frac{b}{ax + b} \right] + C$

10.  $\int \frac{dx}{x(ax + b)} = \frac{1}{b} \ln \left| \frac{x}{ax + b} \right| + C$

11.  $\int (\sqrt{ax + b})^n \, dx = \frac{2}{a} \frac{(\sqrt{ax + b})^{n+2}}{n+2} + C, \quad n \neq -2$

12.  $\int \frac{\sqrt{ax + b}}{x} \, dx = 2\sqrt{ax + b} + b \int \frac{dx}{x\sqrt{ax + b}}$

13. (a)  $\int \frac{dx}{x\sqrt{ax + b}} = \frac{2}{\sqrt{-b}} \tan^{-1} \sqrt{\frac{ax + b}{-b}} + C, \quad \text{if } b < 0$

(b)  $\int \frac{dx}{x\sqrt{ax + b}} = \frac{1}{\sqrt{b}} \ln \left| \frac{\sqrt{ax + b} - \sqrt{b}}{\sqrt{ax + b} + \sqrt{b}} \right| + C, \quad \text{if } b > 0$

14.  $\int \frac{\sqrt{ax + b}}{x^2} \, dx = -\frac{\sqrt{ax + b}}{x} + \frac{a}{2} \int \frac{dx}{x\sqrt{ax + b}} + C$

15.  $\int \frac{dx}{x^2\sqrt{ax + b}} = -\frac{\sqrt{ax + b}}{bx} - \frac{a}{2b} \int \frac{dx}{x\sqrt{ax + b}} + C$

16.  $\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$

17.  $\int \frac{dx}{(a^2 + x^2)^2} = \frac{x}{2a^2(a^2 + x^2)} + \frac{1}{2a^3} \tan^{-1} \frac{x}{a} + C$

18.  $\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left| \frac{x + a}{x - a} \right| + C$

19.  $\int \frac{dx}{(a^2 - x^2)^2} = \frac{x}{2a^2(a^2 - x^2)} + \frac{1}{2a^2} \int \frac{dx}{a^2 - x^2}$

20.  $\int \frac{dx}{\sqrt{a^2 + x^2}} = \sinh^{-1} \frac{x}{a} + C = \ln(x + \sqrt{a^2 + x^2}) + C$

21.  $\int \sqrt{a^2 + x^2} dx = \frac{x}{2}\sqrt{a^2 + x^2} + \frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2}) + C$

22.  $\int x^2 \sqrt{a^2 + x^2} dx = \frac{x}{8}(a^2 + 2x^2)\sqrt{a^2 + x^2} - \frac{a^4}{8} \ln(x + \sqrt{a^2 + x^2}) + C$

23.  $\int \frac{\sqrt{a^2 + x^2}}{x} dx = \sqrt{a^2 + x^2} - a \ln \left| \frac{a + \sqrt{a^2 + x^2}}{x} \right| + C$

24.  $\int \frac{\sqrt{a^2 + x^2}}{x^2} dx = \ln(x + \sqrt{a^2 + x^2}) - \frac{\sqrt{a^2 + x^2}}{x} + C$

25.  $\int \frac{x^2}{\sqrt{a^2 + x^2}} dx = -\frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2}) + \frac{x\sqrt{a^2 + x^2}}{2} + C$

26.  $\int \frac{dx}{x\sqrt{a^2 + x^2}} = -\frac{1}{a} \ln \left| \frac{a + \sqrt{a^2 + x^2}}{x} \right| + C$

27.  $\int \frac{dx}{x^2\sqrt{a^2 + x^2}} = -\frac{\sqrt{a^2 + x^2}}{a^2 x} + C$

28.  $\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C$

29.  $\int \sqrt{a^2 - x^2} dx = \frac{x}{2}\sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} + C$

30.  $\int x^2 \sqrt{a^2 - x^2} dx = \frac{a^4}{8} \sin^{-1} \frac{x}{a} - \frac{1}{8}x\sqrt{a^2 - x^2}(a^2 - 2x^2) + C$

31.  $\int \frac{\sqrt{a^2 - x^2}}{x} dx = \sqrt{a^2 - x^2} - a \ln \left| \frac{a + \sqrt{a^2 - x^2}}{x} \right| + C$

32.  $\int \frac{\sqrt{a^2 - x^2}}{x^2} dx = -\sin^{-1} \frac{x}{a} - \frac{\sqrt{a^2 - x^2}}{x} + C$

33.  $\int \frac{x^2}{\sqrt{a^2 - x^2}} dx = \frac{a^2}{2} \sin^{-1} \frac{x}{a} - \frac{1}{2}x\sqrt{a^2 - x^2} + C$

34.  $\int \frac{dx}{x\sqrt{a^2 - x^2}} = -\frac{1}{a} \ln \left| \frac{a + \sqrt{a^2 - x^2}}{x} \right| + C$

35.  $\int \frac{dx}{x^2\sqrt{a^2 - x^2}} = -\frac{\sqrt{a^2 - x^2}}{a^2 x} + C$

36.  $\int \frac{dx}{\sqrt{x^2 - a^2}} = \cosh^{-1} \frac{x}{a} + C = \ln|x + \sqrt{x^2 - a^2}| + C$

37.  $\int \sqrt{x^2 - a^2} dx = \frac{x}{2}\sqrt{x^2 - a^2} - \frac{a^2}{2} \ln|x + \sqrt{x^2 - a^2}| + C$

38.  $\int (\sqrt{x^2 - a^2})^n dx = \frac{x(\sqrt{x^2 - a^2})^n}{n+1} - \frac{na^2}{n+1} \int (\sqrt{x^2 - a^2})^{n-2} dx, \quad n \neq -1$

39.  $\int \frac{dx}{(\sqrt{x^2 - a^2})^n} = \frac{x(\sqrt{x^2 - a^2})^{2-n}}{(2-n)a^2} - \frac{n-3}{(n-2)a^2} \int \frac{dx}{(\sqrt{x^2 - a^2})^{n-2}}, \quad n \neq 2$

40.  $\int x(\sqrt{x^2 - a^2})^n dx = \frac{(\sqrt{x^2 - a^2})^{n+2}}{n+2} + C, \quad n \neq -2$

41.  $\int x^2 \sqrt{x^2 - a^2} dx = \frac{x}{8}(2x^2 - a^2)\sqrt{x^2 - a^2} - \frac{a^4}{8} \ln|x + \sqrt{x^2 - a^2}| + C$

42.  $\int \frac{\sqrt{x^2 - a^2}}{x} dx = \sqrt{x^2 - a^2} - a \sec^{-1} \left| \frac{x}{a} \right| + C$

43.  $\int \frac{\sqrt{x^2 - a^2}}{x^2} dx = \ln |x + \sqrt{x^2 - a^2}| - \frac{\sqrt{x^2 - a^2}}{x} + C$

44.  $\int \frac{x^2}{\sqrt{x^2 - a^2}} dx = \frac{a^2}{2} \ln |x + \sqrt{x^2 - a^2}| + \frac{x}{2} \sqrt{x^2 - a^2} + C$

45.  $\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C = \frac{1}{a} \cos^{-1} \left| \frac{a}{x} \right| + C$

46.  $\int \frac{dx}{x^2\sqrt{x^2 - a^2}} = \frac{\sqrt{x^2 - a^2}}{a^2 x} + C$

47.  $\int \frac{dx}{\sqrt{2ax - x^2}} = \sin^{-1} \left( \frac{x - a}{a} \right) + C$

48.  $\int \sqrt{2ax - x^2} dx = \frac{x - a}{2} \sqrt{2ax - x^2} + \frac{a^2}{2} \sin^{-1} \left( \frac{x - a}{a} \right) + C$

49.  $\int (\sqrt{2ax - x^2})^n dx = \frac{(x - a)(\sqrt{2ax - x^2})^n}{n + 1} + \frac{na^2}{n + 1} \int (\sqrt{2ax - x^2})^{n-2} dx$

50.  $\int \frac{dx}{(\sqrt{2ax - x^2})^n} = \frac{(x - a)(\sqrt{2ax - x^2})^{2-n}}{(n - 2)a^2} + \frac{(n - 3)}{(n - 2)a^2} \int \frac{dx}{(\sqrt{2ax - x^2})^{n-2}}$

51.  $\int x\sqrt{2ax - x^2} dx = \frac{(x + a)(2x - 3a)\sqrt{2ax - x^2}}{6} + \frac{a^3}{2} \sin^{-1} \left( \frac{x - a}{a} \right) + C$

52.  $\int \frac{\sqrt{2ax - x^2}}{x} dx = \sqrt{2ax - x^2} + a \sin^{-1} \left( \frac{x - a}{a} \right) + C$

53.  $\int \frac{\sqrt{2ax - x^2}}{x^2} dx = -2\sqrt{\frac{2a - x}{x}} - \sin^{-1} \left( \frac{x - a}{a} \right) + C$

54.  $\int \frac{x dx}{\sqrt{2ax - x^2}} = a \sin^{-1} \left( \frac{x - a}{a} \right) - \sqrt{2ax - x^2} + C$

55.  $\int \frac{dx}{x\sqrt{2ax - x^2}} = -\frac{1}{a} \sqrt{\frac{2a - x}{x}} + C$

56.  $\int \sin ax dx = -\frac{1}{a} \cos ax + C$

57.  $\int \cos ax dx = \frac{1}{a} \sin ax + C$

58.  $\int \sin^2 ax dx = \frac{x}{2} - \frac{\sin 2ax}{4a} + C$

59.  $\int \cos^2 ax dx = \frac{x}{2} + \frac{\sin 2ax}{4a} + C$

60.  $\int \sin^n ax dx = -\frac{\sin^{n-1} ax \cos ax}{na} + \frac{n-1}{n} \int \sin^{n-2} ax dx$

61.  $\int \cos^n ax dx = \frac{\cos^{n-1} ax \sin ax}{na} + \frac{n-1}{n} \int \cos^{n-2} ax dx$

62. (a)  $\int \sin ax \cos bx dx = -\frac{\cos(a+b)x}{2(a+b)} - \frac{\cos(a-b)x}{2(a-b)} + C, \quad a^2 \neq b^2$

(b)  $\int \sin ax \sin bx dx = \frac{\sin(a-b)x}{2(a-b)} - \frac{\sin(a+b)x}{2(a+b)} + C, \quad a^2 \neq b^2$

(c)  $\int \cos ax \cos bx dx = \frac{\sin(a-b)x}{2(a-b)} + \frac{\sin(a+b)x}{2(a+b)} + C, \quad a^2 \neq b^2$

63.  $\int \sin ax \cos ax \, dx = -\frac{\cos 2ax}{4a} + C$

64.  $\int \sin^n ax \cos ax \, dx = \frac{\sin^{n+1} ax}{(n+1)a} + C, \quad n \neq -1$

65.  $\int \frac{\cos ax}{\sin ax} \, dx = \frac{1}{a} \ln |\sin ax| + C$

66.  $\int \cos^n ax \sin ax \, dx = -\frac{\cos^{n+1} ax}{(n+1)a} + C, \quad n \neq -1$

67.  $\int \frac{\sin ax}{\cos ax} \, dx = -\frac{1}{a} \ln |\cos ax| + C$

68.  $\int \sin^n ax \cos^m ax \, dx = -\frac{\sin^{n-1} ax \cos^{m+1} ax}{a(m+n)} + \frac{n-1}{m+n} \int \sin^{n-2} ax \cos^m ax \, dx, \quad n \neq -m \quad (\text{If } n = -m, \text{ use No. 86.})$

69.  $\int \sin^n ax \cos^m ax \, dx = \frac{\sin^{n+1} ax \cos^{m-1} ax}{a(m+n)} + \frac{m-1}{m+n} \int \sin^n ax \cos^{m-2} ax \, dx, \quad m \neq -n \quad (\text{If } m = -n, \text{ use No. 87.})$

70.  $\int \frac{dx}{b+c \sin ax} = \frac{-2}{a\sqrt{b^2-c^2}} \tan^{-1} \left[ \sqrt{\frac{b-c}{b+c}} \tan \left( \frac{\pi}{4} - \frac{ax}{2} \right) \right] + C, \quad b^2 > c^2$

71.  $\int \frac{dx}{b+c \sin ax} = \frac{-1}{a\sqrt{c^2-b^2}} \ln \left| \frac{c+b \sin ax + \sqrt{c^2-b^2} \cos ax}{b+c \sin ax} \right| + C, \quad b^2 < c^2$

72.  $\int \frac{dx}{1+\sin ax} = -\frac{1}{a} \tan \left( \frac{\pi}{4} - \frac{ax}{2} \right) + C$

73.  $\int \frac{dx}{1-\sin ax} = \frac{1}{a} \tan \left( \frac{\pi}{4} + \frac{ax}{2} \right) + C$

74.  $\int \frac{dx}{b+c \cos ax} = \frac{2}{a\sqrt{b^2-c^2}} \tan^{-1} \left[ \sqrt{\frac{b-c}{b+c}} \tan \frac{ax}{2} \right] + C, \quad b^2 > c^2$

75.  $\int \frac{dx}{b+c \cos ax} = \frac{1}{a\sqrt{c^2-b^2}} \ln \left| \frac{c+b \cos ax + \sqrt{c^2-b^2} \sin ax}{b+c \cos ax} \right| + C, \quad b^2 < c^2$

76.  $\int \frac{dx}{1+\cos ax} = \frac{1}{a} \tan \frac{ax}{2} + C$

77.  $\int \frac{dx}{1-\cos ax} = -\frac{1}{a} \cot \frac{ax}{2} + C$

78.  $\int x \sin ax \, dx = \frac{1}{a^2} \sin ax - \frac{x}{a} \cos ax + C$

79.  $\int x \cos ax \, dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax + C$

80.  $\int x^n \sin ax \, dx = -\frac{x^n}{a} \cos ax + \frac{n}{a} \int x^{n-1} \cos ax \, dx$

81.  $\int x^n \cos ax \, dx = \frac{x^n}{a} \sin ax - \frac{n}{a} \int x^{n-1} \sin ax \, dx$

82.  $\int \tan ax \, dx = \frac{1}{a} \ln |\sec ax| + C$

83.  $\int \cot ax \, dx = \frac{1}{a} \ln |\sin ax| + C$

84.  $\int \tan^2 ax \, dx = \frac{1}{a} \tan ax - x + C$

85.  $\int \cot^2 ax \, dx = -\frac{1}{a} \cot ax - x + C$

86.  $\int \tan^n ax \, dx = \frac{\tan^{n-1} ax}{a(n-1)} - \int \tan^{n-2} ax \, dx, \quad n \neq 1$

87.  $\int \cot^n ax \, dx = -\frac{\cot^{n-1} ax}{a(n-1)} - \int \cot^{n-2} ax \, dx, \quad n \neq 1$

88.  $\int \sec ax \, dx = \frac{1}{a} \ln |\sec ax + \tan ax| + C$

89.  $\int \csc ax \, dx = -\frac{1}{a} \ln |\csc ax - \cot ax| + C$

90.  $\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$

91.  $\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$

92. 
$$\int \sec^n ax dx = \frac{\sec^{n-2} ax \tan ax}{a(n-1)} + \frac{n-2}{n-1} \int \sec^{n-2} ax dx, \quad n \neq 1$$

93. 
$$\int \csc^n ax dx = -\frac{\csc^{n-2} ax \cot ax}{a(n-1)} + \frac{n-2}{n-1} \int \csc^{n-2} ax dx, \quad n \neq 1$$

94. 
$$\int \sec^n ax \tan ax dx = \frac{\sec^n ax}{na} + C, \quad n \neq 0$$

95. 
$$\int \csc^n ax \cot ax dx = -\frac{\csc^n ax}{na} + C, \quad n \neq 0$$

96. 
$$\int \sin^{-1} ax dx = x \sin^{-1} ax + \frac{1}{a} \sqrt{1-a^2x^2} + C$$

97. 
$$\int \cos^{-1} ax dx = x \cos^{-1} ax - \frac{1}{a} \sqrt{1-a^2x^2} + C$$

98. 
$$\int \tan^{-1} ax dx = x \tan^{-1} ax - \frac{1}{2a} \ln(1+a^2x^2) + C$$

99. 
$$\int x^n \sin^{-1} ax dx = \frac{x^{n+1}}{n+1} \sin^{-1} ax - \frac{a}{n+1} \int \frac{x^{n+1} dx}{\sqrt{1-a^2x^2}}, \quad n \neq -1$$

100. 
$$\int x^n \cos^{-1} ax dx = \frac{x^{n+1}}{n+1} \cos^{-1} ax + \frac{a}{n+1} \int \frac{x^{n+1} dx}{\sqrt{1-a^2x^2}}, \quad n \neq -1$$

101. 
$$\int x^n \tan^{-1} ax dx = \frac{x^{n+1}}{n+1} \tan^{-1} ax - \frac{a}{n+1} \int \frac{x^{n+1} dx}{1+a^2x^2}, \quad n \neq -1$$

102. 
$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

103. 
$$\int b^{ax} dx = \frac{1}{a} \frac{b^{ax}}{\ln b} + C, \quad b > 0, \quad b \neq 1$$

104. 
$$\int xe^{ax} dx = \frac{e^{ax}}{a^2}(ax-1) + C$$

105. 
$$\int x^n e^{ax} dx = \frac{1}{a} x^n e^{ax} - \frac{n}{a} \int x^{n-1} e^{ax} dx$$

106. 
$$\int x^n b^{ax} dx = \frac{x^n b^{ax}}{a \ln b} - \frac{n}{a \ln b} \int x^{n-1} b^{ax} dx, \quad b > 0, \quad b \neq 1$$

107. 
$$\int e^{ax} \sin bx dx = \frac{e^{ax}}{a^2+b^2} (a \sin bx - b \cos bx) + C$$

108. 
$$\int e^{ax} \cos bx dx = \frac{e^{ax}}{a^2+b^2} (a \cos bx + b \sin bx) + C$$

109. 
$$\int \ln ax dx = x \ln ax - x + C$$

110. 
$$\int x^n (\ln ax)^m dx = \frac{x^{n+1} (\ln ax)^m}{n+1} - \frac{m}{n+1} \int x^n (\ln ax)^{m-1} dx, \quad n \neq -1$$

111. 
$$\int x^{-1} (\ln ax)^m dx = \frac{(\ln ax)^{m+1}}{m+1} + C, \quad m \neq -1$$

112. 
$$\int \frac{dx}{x \ln ax} = \ln |\ln ax| + C$$

113. 
$$\int \sinh ax dx = \frac{1}{a} \cosh ax + C$$

114. 
$$\int \cosh ax dx = \frac{1}{a} \sinh ax + C$$

115. 
$$\int \sinh^2 ax dx = \frac{\sinh 2ax}{4a} - \frac{x}{2} + C$$

116. 
$$\int \cosh^2 ax dx = \frac{\sinh 2ax}{4a} + \frac{x}{2} + C$$

117. 
$$\int \sinh^n ax dx = \frac{\sinh^{n-1} ax \cosh ax}{na} - \frac{n-1}{n} \int \sinh^{n-2} ax dx, \quad n \neq 0$$

$$118. \int \cosh^n ax dx = \frac{\cosh^{n-1} ax \sinh ax}{na} + \frac{n-1}{n} \int \cosh^{n-2} ax dx, \quad n \neq 0$$

$$119. \int x \sinh ax dx = \frac{x}{a} \cosh ax - \frac{1}{a^2} \sinh ax + C$$

$$121. \int x^n \sinh ax dx = \frac{x^n}{a} \cosh ax - \frac{n}{a} \int x^{n-1} \cosh ax dx$$

$$123. \int \tanh ax dx = \frac{1}{a} \ln(\cosh ax) + C$$

$$125. \int \tanh^2 ax dx = x - \frac{1}{a} \tanh ax + C$$

$$127. \int \tanh^n ax dx = -\frac{\tanh^{n-1} ax}{(n-1)a} + \int \tanh^{n-2} ax dx, \quad n \neq 1$$

$$128. \int \coth^n ax dx = -\frac{\coth^{n-1} ax}{(n-1)a} + \int \coth^{n-2} ax dx, \quad n \neq 1$$

$$129. \int \operatorname{sech} ax dx = \frac{1}{a} \sin^{-1}(\tanh ax) + C$$

$$131. \int \operatorname{sech}^2 ax dx = \frac{1}{a} \tanh ax + C$$

$$133. \int \operatorname{sech}^n ax dx = \frac{\operatorname{sech}^{n-2} ax \tanh ax}{(n-1)a} + \frac{n-2}{n-1} \int \operatorname{sech}^{n-2} ax dx, \quad n \neq 1$$

$$134. \int \operatorname{csch}^n ax dx = -\frac{\operatorname{csch}^{n-2} ax \coth ax}{(n-1)a} - \frac{n-2}{n-1} \int \operatorname{csch}^{n-2} ax dx, \quad n \neq 1$$

$$135. \int \operatorname{sech}^n ax \tanh ax dx = -\frac{\operatorname{sech}^n ax}{na} + C, \quad n \neq 0$$

$$137. \int e^{ax} \sinh bx dx = \frac{e^{ax}}{2} \left[ \frac{e^{bx}}{a+b} - \frac{e^{-bx}}{a-b} \right] + C, \quad a^2 \neq b^2$$

$$138. \int e^{ax} \cosh bx dx = \frac{e^{ax}}{2} \left[ \frac{e^{bx}}{a+b} + \frac{e^{-bx}}{a-b} \right] + C, \quad a^2 \neq b^2$$

$$139. \int_0^\infty x^{n-1} e^{-x} dx = (n-1)!, \quad n > 0$$

$$141. \int_0^{\pi/2} \sin^n x dx = \int_0^{\pi/2} \cos^n x dx = \begin{cases} \frac{1 \cdot 3 \cdot 5 \cdots (n-1)}{2 \cdot 4 \cdot 6 \cdots n} \cdot \frac{\pi}{2}, & \text{if } n \text{ is an even integer } \geq 2 \\ \frac{2 \cdot 4 \cdot 6 \cdots (n-1)}{3 \cdot 5 \cdot 7 \cdots n}, & \text{if } n \text{ is an odd integer } \geq 3 \end{cases}$$

$$120. \int x \cosh ax dx = \frac{x}{a} \sinh ax - \frac{1}{a^2} \cosh ax + C$$

$$122. \int x^n \cosh ax dx = \frac{x^n}{a} \sinh ax - \frac{n}{a} \int x^{n-1} \sinh ax dx$$

$$124. \int \coth ax dx = \frac{1}{a} \ln |\sinh ax| + C$$

$$126. \int \coth^2 ax dx = x - \frac{1}{a} \coth ax + C$$

$$130. \int \operatorname{csch} ax dx = \frac{1}{a} \ln \left| \tanh \frac{ax}{2} \right| + C$$

$$132. \int \operatorname{csch}^2 ax dx = -\frac{1}{a} \coth ax + C$$

$$136. \int \operatorname{csch}^n ax \coth ax dx = -\frac{\operatorname{csch}^n ax}{na} + C, \quad n \neq 0$$

$$140. \int_0^\infty e^{-ax^2} dx = \frac{1}{2} \sqrt{\frac{\pi}{a}}, \quad a > 0$$